

[0041] Using the following formula, inverse discrete fractional Fourier $b=[b(0),b(1), \dots, b(N-1)]$ of B can be obtained:

$$b(n) = \text{IDFrFT}\{B(m)\} = \sqrt{\frac{\sin\alpha + j\cos\alpha}{N}} e^{-j\frac{1}{2}\cot\alpha n^2 \Delta t^2} \sum_{m=0}^{N-1} B(m) e^{j\frac{2\pi}{N} mn} e^{-j\frac{1}{2}\cot\alpha m^2 \Delta t^2} \quad (15)$$

$$n = 0, 1, \dots, N-1$$

[0042] The formula (11) and the formula (12) are brought into the formula (13):

$$b(n) = N \sqrt{\frac{\sin\alpha + j\cos\alpha}{N}} e^{-j\frac{1}{2}\cot\alpha (iM)^2 \Delta t^2} \sum_{i=0}^{L-1} r(i) \delta(n - iM) \quad (16)$$

$$n = 0, 1, \dots, N-1$$

wherein $r(i)=\text{IDFT}\{R(m)\}$. From the formula (14) can be seen that sequence B with N -length. After inverse discrete fractional Fourier transform of B , the time domain $b^{(l)}$ sequence is obtained which is only related to $r^{(l)}(i)$, and the number of non-zero is only L .

[0043] B. The Method of Low Complexity PAPR Suppression

[0044] As the basic principles of SLM method, multiply alternative random phase sequence B whose number is S is multiplied by the data before subcarrier modulation, and then alternative signals $X^{(l)}$ whose number is S can be obtained:

$$X^{(l)} = X \square B^{(l)} [X(0) \square B^{(l)}(0), X(1) \square B^{(l)}(1), \dots, X(N-1) \square B^{(l)}(N-1)], l=1, 2, \dots, S \quad (17)$$

[0045] Then, make these alternatives IDFrFT, and obtain alternative signal $\bar{X}^{(l)}$ whose the number is S of time-domain FRFT-OFDM.

$$\bar{X}^{(l)} = \text{IDFrFT}\{X^{(l)}\} \quad (18)$$

[0046] Fractional circular convolution theorem:

[0047] If

$$\bar{X}^{(l)} = X \square B^{(l)} e^{j\frac{1}{2}\cot\alpha m^2 \Delta t^2} \quad (19a)$$

Then

$$\bar{X}^{(l)} = x \otimes_p^N b^{(l)} \quad (19b)$$

[0048] Which:

$$\otimes_p^N$$

is n -point circular convolution Fractional with p -order. x is N -point inverse discrete fractional Fourier transform of X ; $b^{(l)}$ is an N -point inverse discrete fractional Fourier transform of $B^{(l)}$. Contrast formula (15) and formula (17.a), $\bar{X}^{(l)}$ need to be amended.

[0049] Make

$$\bar{X}^{(l)}(m) = \bar{X}^{(l)}(m) \square e^{j\frac{1}{2}\cot\alpha m^2 \Delta t^2}$$

(after receiving end making DFrFT, $\bar{X}^{(l)}$ can be obtained easily by multiplied a phase factor

$$e^{j\frac{1}{2}\cot\alpha (m)^2 \Delta t^2})$$

as the candidate signals of this method. And then N -point IDFrFT of $\square \bar{X}^{(l)}$ is:

$$\bar{X}^{(l)} \bar{X}^{(l)} = \text{IDFrFT}\{\bar{X}^{(l)}\} = x \otimes_p^N b^{(l)} \quad (20)$$

[0050] Due to expression of $b^{(l)} = \{b^{(l)}(0), b^{(l)}(1), \dots, b^{(l)}(N-1)\}$

$$b^{(l)}(n) = N \sqrt{\frac{\sin\alpha + j\cos\alpha}{N}} e^{j\frac{1}{2}\cot\alpha (iM)^2 \Delta t^2} \sum_{i=0}^{L-1} r(i) \delta(n - iM) \quad (21)$$

$$n = 0, 1, \dots, N-1, l = 1, 2, \dots, S$$

wherein $r^{(l)}(i)=\text{IDFT}\{R^{(l)}(m)\}$. Bring formula (19) into the formula (18) can obtain:

$$\bar{X}^{(l)}(n) = \sum_{i=0}^{L-1} r^{(l)}(i) \square x((n - iM))_{P,N} \square R_N(n) \square e^{j\frac{1}{2}\cot\alpha [-2iM \square n + (iM)^2] \Delta t^2} \quad (22)$$

$$n = 0, 1, \dots, N-1, l = 1, 2, \dots, S$$

wherein $R_N(n) = \begin{cases} 1 & 1 \leq n \leq N-1 \\ 0 & \text{other} \end{cases}$

is the value of the primary value range; $x((n-iM))_{P,N} R_N(n)$ is a signal which is obtained by periodic extension of chirp with N -cycle and p -order, and then carry it on a circular movement. That is, according to the formula (21) shows the cycle of the chirp, $x((n))_{P,N}$ can be obtained by periodic extension of chirp.

[0051] That is, according to the formula (21) the chirp cycle is shown, the X is extended to the chirp cycle, then the P is shifted and the main value range is taken.

$$x(n-N) e^{j\frac{1}{2}\cot\alpha (n-N)^2 \Delta t^2} = x(n) e^{-j\frac{1}{2}\cot\alpha n^2 \Delta t^2} \quad (23)$$

[0052] Making

$$\eta(n, i) = e^{j\frac{1}{2}\cot\alpha [-2iM \square n + (iM)^2] \Delta t^2},$$

then $\eta(n,0)=1$, formula (20) can expressed as formula (22).